TOPIC 1
INTRODUCING SOME MATHEMATICS SOFTWARE
(Matlab, Maple and Mathematica)

This topic provides information about some mathematics software. Some of those are MATLAB, Maple, and Mathematica. The software has specific function, but some of them have the same function. Below is brief description about the software.

A. MATLAB

The name MATLAB stands for matrix laboratory. The software has many features such 2-D and 3-D graphics functions for visualizing data, Mathematical functions for linear algebra, statistics and Fourier analysis.

Basic MATLAB features
To run MATLAB, go to Start ➔ Program ➔ Matlab.
Running MATLAB creatures one or more windows on your computer monitor. Of these, the command window is the primary place where you interact with MATLAB.

Figure 1. Command window in Matlab
**Definition of Variables**

Variables are assigned numerical values by typing the expression directly, for example, typing

```plaintext
>> a = 1+2
```

yields:

```
a = 
```

3

The answer will not be displayed when a semicolon is put at the end of an expression, for example type

```plaintext
>> a = 1+2;
```

MATLAB utilizes the following arithmetic operators:

```
+ addition
- subtraction
* multiplication
/ division
^ power operator
' transpose
```

A variable can be assigned using a formula that utilizes these operators and either numbers or previously defined variables. For example, since `a` was defined previously, the following expression is valid

```plaintext
>> b = 2*a;
```

To determine the value of a previously defined quantity, type the quantity by itself:

```plaintext
>> b
```

yields:

```
b = 
```

6

If your expression does not fit on one line, use an ellipsis (three or more periods at the end of the line) and continue on the next line.

```plaintext
>> c = 1+2+3+... 5+6+7;
```

MATLAB has rules about variables names, which are:

<table>
<thead>
<tr>
<th>Variables naming rules</th>
<th>Comments/examples</th>
</tr>
</thead>
<tbody>
<tr>
<td>Variables names must be single word containing no space</td>
<td>cost, average_cost</td>
</tr>
<tr>
<td>Variables names are case sensitive</td>
<td>Items, items, iTems and ITEMS are all different</td>
</tr>
<tr>
<td>Variables names can contain up to 19 characters; characters beyond the 19th are ignored</td>
<td>Howaboutthisvariblename</td>
</tr>
<tr>
<td>Variables names must start with a letter, followed by any number of letters, digits, or underscores.</td>
<td>How_about_this_variable X123</td>
</tr>
<tr>
<td>Punctuation characters are not allowed</td>
<td>Punctuation characters have many special meaning to MATLAB</td>
</tr>
<tr>
<td>Not special variables which predefined in MATLAB</td>
<td>ans, pi, eps, flops, inf, NaN, i (dan) j, nargin, nargout, realmin, realmax</td>
</tr>
</tbody>
</table>
There are several predefined variables which can be used at any time, in the same manner as user defined variables:

\begin{align*}
i &\equiv \sqrt{-1} \\
j &\equiv \sqrt{-1} \\
p_i &\equiv 3.1416... \\
\end{align*}

For example,

\begin{verbatim}
>> y = 2*(1+4*j)
yields: y = 2.0000 + 8.0000i
\end{verbatim}

\textbf{Tip1}: To recall previous commands, use the cursor key \[\uparrow\] on your keyboard.

\textbf{Tip2}: Entering the first few characters of a known previous command at the prompt, and then pressing the \[\uparrow\] key, immediately recalls the most recent command having those initial characters.

\textbf{Tip3}: The command can be edited by using the \[\uparrow\] key to recall the command and then use the \[\leftarrow\] and \[\rightarrow\] key to move the cursor within the command at the MATLAB prompt.

The MATLAB help command is the simplest way to get help if you know the topic you want help on. Typing \texttt{help topic} displays help about that topic if it exists.

\begin{verbatim}
>> help sqrt
\end{verbatim}

As an alternative to getting help in the command window, menu-driven help may be available from the Menu Bar.

\section*{B. MAPLE}

Maple is an educational math software program by Waterloo Maple Inc. Maple is comprehensive math software package for engineers, scientists, educators, researchers, teachers, and students. With the software, user can do many things in mathematics, including calculus, statistics, algebra, differential equations, linear algebra, geometry, transforms, plotting in 2D and 3D and more.

\textbf{How to start and exit Maple}

To start maple: Go to Start Menu -> Programs -> Maple 8 -> Maple 8.
To exit Maple, choose File -> Exit.

**Some Basic Maple Commands**

After you log on to your terminal and access Maple, you will get a window containing a "prompt" > where you can immediately begin entering Maple commands. If you wanted to multiply the numbers 247 and 3756, you would enter

> 247*3756;

NOTE: Every Maple V command must end with either a semicolon or a colon. If a command is ended with a colon then the calculation will be made but no output will be printed. When a semicolon is used the calculation will be made and the result will be printed.

If a colon were used on the previous command, the result would look like the following:

> 247*3756:

If the semicolon or colon is omitted from a command, the command will not execute. Maple will respond as follows:

> 247*3756

*Warning, premature end of input*

However, because Maple allows full screen editing, you can go back to the line where the problem occurred and correct it.

**Maple Syntax and Built-in Data Capabilities**

**Syntax**

As with any computer language, Maple has its own syntax. As a new user of Maple, you can save yourself a lot of head-scratching if you get to know these symbols.
Enter the commands given or make up similar problems.

<table>
<thead>
<tr>
<th>Symbol</th>
<th>Description</th>
<th>Examples</th>
<th>Sample Output</th>
</tr>
</thead>
<tbody>
<tr>
<td>;</td>
<td>End-of-line. Tells Maple to process the line and show the output.</td>
<td>hello;</td>
<td>hello</td>
</tr>
<tr>
<td>;</td>
<td>End-of-line. Tells Maple to process the line and hide the output.</td>
<td>hello;</td>
<td></td>
</tr>
<tr>
<td>:=</td>
<td>Assignment. Lets you assign values to variables.</td>
<td>a := 3; a;</td>
<td>a := 3 3</td>
</tr>
<tr>
<td>+, -</td>
<td>Addition, subtraction.</td>
<td>1 + 3; 1 - 3;</td>
<td>4 -2</td>
</tr>
<tr>
<td>* , /</td>
<td>Multiplication, division</td>
<td>3*412; 1236/3; 7/3;</td>
<td>1236 412 7/3</td>
</tr>
</tbody>
</table>

| ^, sqrt | Power, square root | 2^3; sqrt(2); 2^(1/2); | 8 $\sqrt{2}$ |
| evalf, . | Floating-point (decimal) evaluation | evalf(7/3); 7.0/3; | 2.333333333 2.333333333 |
| I, Pi  | Imaginary number, Pi. | 2 + 3*I; (2*I)^2; evalf(Pi); | 2+3I 3.141592654 |
| %, %% | Recall the last output, recall the second-to-last output, etc. | %; %%%; | 3.141592654 -4 |

**Built-in Data Capabilities**

Maple can handle arbitrary-precision floating point numbers. In other words, Maple can store as many digits for a number as you like, up to the physical limits of your computer's memory. To control this, use the Digits variable.

```
> sqrt(2.0);
1.414213562
> Digits := 20:
> sqrt(2.0);
1.4142135623730950488
```

Maple sets Digits to be 10 by default. You can also temporarily get precision results by calling evalf with a second argument.
> evalf(sqrt(2), 15);
1.41421356237310
Large integers are handled automatically.

The Kernel
The kernel is the part of Maple that does the actual calculation. The kernel is invisible, but you do need to know about it. You talk to the kernel by typing mathematical statements and commands at the Maple prompt. Here is an example.

```
> a := 5;
  a := 5
```

If you're using a graphics-enabled browser, you'll notice that input appears in red. Output from the kernel appears in blue, with variable names in italics. The Maple prompt looks like `>`. The kernel will execute when you press the Enter key. The kernel decides what to execute by looking at the current execution group. An execution group is a set of input lines connected (along the left-hand margin) by a long, thin ``. When you press Enter anywhere in the execution group, the entire group is executed. By default, each input line (along with its output) is an execution group unto itself. You can join execution groups together using the F4 key, or split them apart using the F3 key.

Worksheets
The worksheet is the basic unit of work in Maple, like a document in a word processor. A worksheet stores every line of input and every line of output. To save your worksheet, choose File->Save As. To open a worksheet, choose File->Open.

You may have more than one worksheet open at a time. However, they all share the same kernel. So any work you do in one worksheet is accessible from another open worksheet. This can lead to confusing results.

Some syntactical caveats:
- Maple is case sensitive. foo, Foo, and FOO are three different things.
- Using the % operator can give confusing results. It always returns the last output from the Kernel, which may have nothing to do with where the cursor is (or which worksheet is active).
- If Maple doesn't recognize something, it will assume it is a variable. For example, typing `i^2` will give you `i2`, while you may have wanted `-1`.
- You can move your cursor up to a previous line, press Enter, and the line will re-execute.
- When copying and pasting using a mouse, be sure to also highlight the execution group symbol (`[]`). If you don't, the lines will be pasted in reverse order due to a bug.
• Spaces are optional.
• Greek letters may be entered by spelling their name. For example, alpha is always displayed as \( \alpha \) and Gamma is displayed as \( \Gamma \) (note upper-case).

Help File
You can obtain the help file regarding most Maple functions and statements by entering \(? name\) where name is the function or statement you desire help on. To see help on factor, you can enter:
\( > \ ? \text{factor} \)
Help can also be obtained using the help option on the toolbar.

C. MATHEMATICA

Wolfram Mathematica is a math software package by Wolfram Research, Inc. is also a powerful math software package. The software allows user do many tasks with mathematics such as do symbolic calculations, create 2D and 3D graphics, do integrals and derivatives, solve equations symbolically and numerically, manipulate vectors and matrices, analyze data.

To start with Mathematica, click Start \( \rightarrow \) Program \( \rightarrow \) Wolfram Mathematica \( \rightarrow \) Wolfram Mathematica 6 Kernel. Mathematica kernel window will appear, as below.

Here some brief examples using Mathematica in mathematics, especially in polynomial, matrices, differentiation, and integration.

Types of Numbers
Four underlying types of numbers are built into Mathematica.
• Integer arbitrary-length exact integer
• Rational \( \text{integer/integer} \) in lowest terms
• Real approximate real number, with any specified precision
• Complex number of the form \( \text{number} + \text{number} \, \text{I} \)

Rational numbers always consist of a ratio of two integers, reduced to lowest terms.

\[
\text{In}[1] := 12 \frac{344}{2222} \\
\text{Out}[1] = 6 \frac{172}{1111}
\]

Approximate real numbers are distinguished by the presence of an explicit decimal point.

\[
\text{In}[2] := 5456. \\
\text{Out}[2] = 5456.
\]

An approximate real number can have any number of digits.

\[
\text{In}[3] := 4.545435234543523453452345234543 \\
\text{Out}[3] = 4.5454352345454352345345234523454
\]

Complex numbers can have integer or rational components.

\[
\text{In}[4] := 4 + \frac{7}{8} \, \text{I} \\
\text{Out}[4] = 4 + \frac{7}{8} \, \text{I}
\]

They can also have approximate real number components.

\[
\text{In}[5] := 4 + 5.6 \, \text{I} \\
\text{Out}[5] = 4 + 5.6 \, \text{I}
\]

You can distinguish different types of numbers in *Mathematica* by looking at their heads.

The object 123 is taken to be an exact integer, with head Integer.

\[
\text{In}[6] := \text{Head}[123] \\
\text{Out}[6] = \text{Integer}
\]

The presence of an explicit decimal point makes *Mathematica* treat 123 as an approximate real number, with head Real.

\[
\text{In}[7] := \text{Head}[123.] \\
\text{Out}[7] = \text{Real}
\]

** Polynomial**

Mathematica provides some commands to finding polynomial, such as:

- \(\text{PolynomialQ}[\text{expr}, x]\) test whether \(\text{expr}\) is a polynomial in \(x\)
- \(\text{PolynomialQ}[\text{expr}, \{x_1, x_2, \ldots\}\] test whether \(\text{expr}\) is a polynomial in the \(x_i\)
- \(\text{Variables}[\text{poly}]\) a list of the variables in \(\text{poly}\)
- \(\text{Exponent}[\text{poly}, x]\) the maximum exponent with which \(x\) appears in \(\text{poly}\)
- \(\text{Coefficient}[\text{poly}, \text{expr}]\) the coefficient of \(\text{expr}\) in \(\text{poly}\)
- \(\text{Coefficient}[\text{poly}, \text{expr}, n]\) the coefficient of \(\text{expr}_n\) in \(\text{poly}\)
- \(\text{Coefficient}[\text{poly}, \text{expr}, 0]\) the term in \(\text{poly}\) independent of \(\text{expr}\)
- \(\text{CoefficientList}[\text{poly}, \{x_1, x_2, \ldots\}\] generate an array of the coefficients of the \(x_i\) in \(\text{poly}\)
- \(\text{CoefficientRules}[\text{poly}, \{x_1, x_2, \ldots\}\] get exponent vectors and coefficients of monomials
Here is a polynomial in two variables.
\[
\text{In}[3]:= \ t = (1 + x)^3 (1 - y - x)^2
\]
\[
\text{Out}[3]= (1 + x)^3 (1 - x - y)^2
\]

This is the polynomial in expanded form.
\[
\text{In}[2]:= \ \text{Expand}[t]
\]
\[
\text{Out}[2]= 1 + x - 2 x^2 - 2 x^3 + x^4 + x^5 - 2 y - 4 x y + 4 x^2 y + 2 x^4 y + y^2 + 3 x y^2 + 3 x^2 y^2 + x^3 y^2
\]

\text{Coefficient}[poly, expr] gives the total coefficient with which expr appears in poly. In this case, the result is a sum of two terms.

\[
\text{In}[3]:= \ \text{Coefficient}[t, x^2]
\]
\[
\text{Out}[3]= -2 + 3 y^2
\]

\textbf{Matrix}

Here some functions for constructing matrices

\[
\begin{align*}
m &= \{(a_{11}, a_{12}, \ldots), (a_{21}, a_{22}, \ldots), \ldots\} & \text{assign } m \text{ to be a matrix} \\
m[[i, j]] &= a & \text{reset element } (i, j) \text{ to be } a \\
m[[i]] &= a & \text{reset all elements in row } i \text{ to be } a \\
m[[i]] &= \{a_1, a_2, \ldots\} & \text{reset elements in row } i \text{ to be } \{a_1, a_2, \ldots\} \\
m[[i_0, i_1]] &= \{v_1, v_2, \ldots\} & \text{reset rows } i_0 \text{ through } i_1 \text{ to be vectors } \{v_1, v_2, \ldots\} \\
m[[A]] &= a & \text{reset all elements in column } j \text{ to be } a \\
m[[A, j]] &= \{a_1, a_2, \ldots\} & \text{reset elements in column } j \text{ to be } \{a_1, a_2, \ldots\} \\
m[[i_0, j_0, i_1, j_1]] &= \{(a_{11}, a_{12}, \ldots), (a_{21}, a_{22}, \ldots), \ldots\} & \text{reset the submatrix with rows } i_0 \text{ through } i_1 \text{ and columns } j_0 \text{ through } j_1 \text{ to new values}
\end{align*}
\]

Here is a 3×3 matrix.
\[
\text{In}[4]:= \ m = \{(a, b, c), (d, e, f), (g, h, i)\}
\]
\[
\text{Out}[4]= \{(a, b, c), (d, e, f), (g, h, i)\}
\]

This resets the 2, 2 element to be x, then shows the whole matrix.
\[
\text{In}[5]:= \ m[[2, 2]] = x; \ m
\]
\[
\text{Out}[5]= \{(a, b, c), (d, x, f), (g, h, i)\}
\]

This increments all the values in the second column.
\[
\text{In}[6]:= \ m[[\text{\{All, 2\}]}]++; \ m
\]
\[
\text{Out}[6]= \{(a, 1 + i, c), (d, 1 + j, f), (g, 1 + k, i)\}
Another examples and feature in mathematica will be leaved as practice for students. You can get help from help menu from wolfram mathematica 6 menus.

To get help menu, click start → program → wolfram mathematica → wolfram mathematica 6. Then click help menu. Choose Documenter center, the window will appear as below.

Click to choose one of topics to get information you needed.