

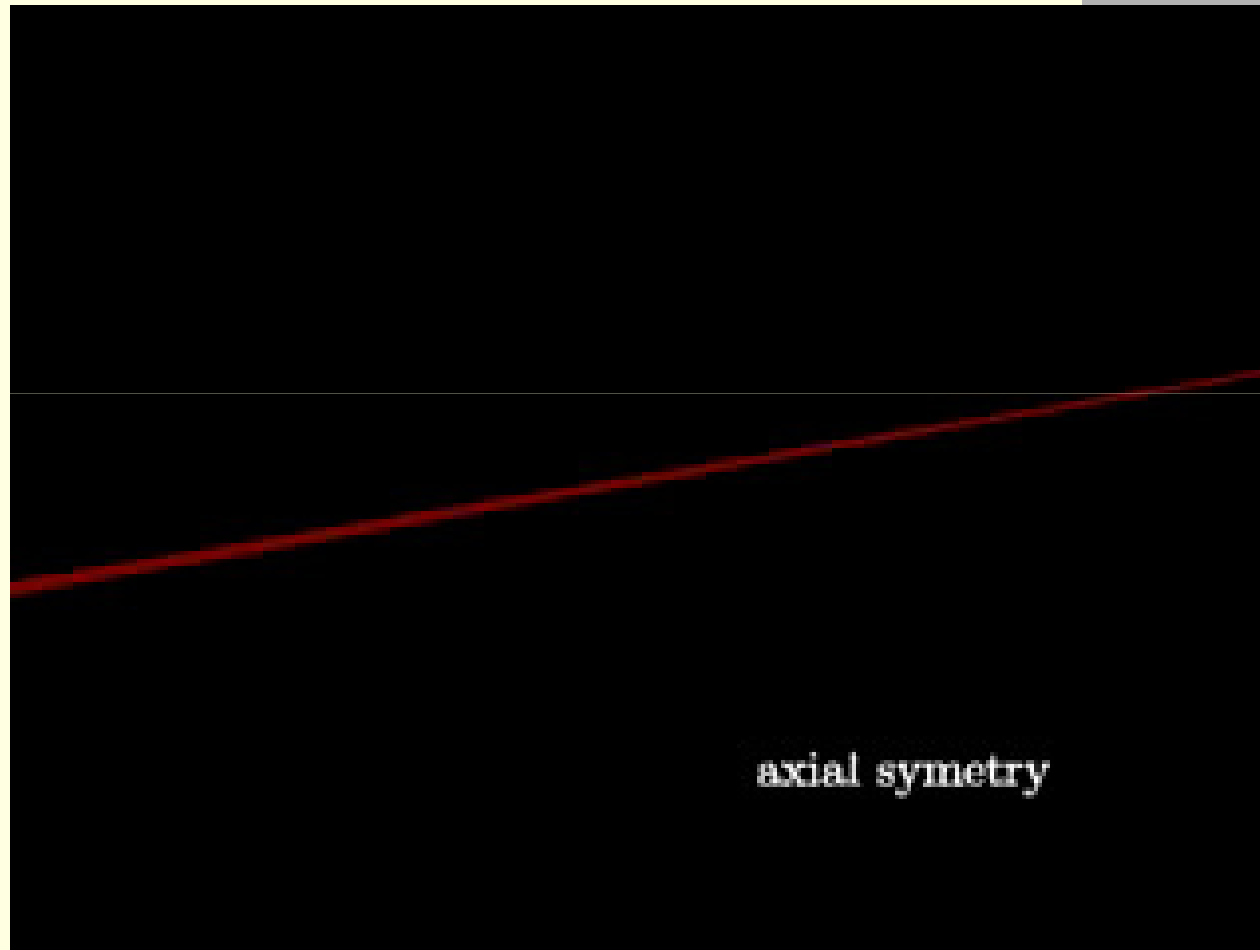
# HUKUM GAUSS

***Oleh :***  
***Sabar Nurohman, M.Pd***



Ke Menu Utama

# Hukum Gauss



axial symmetry

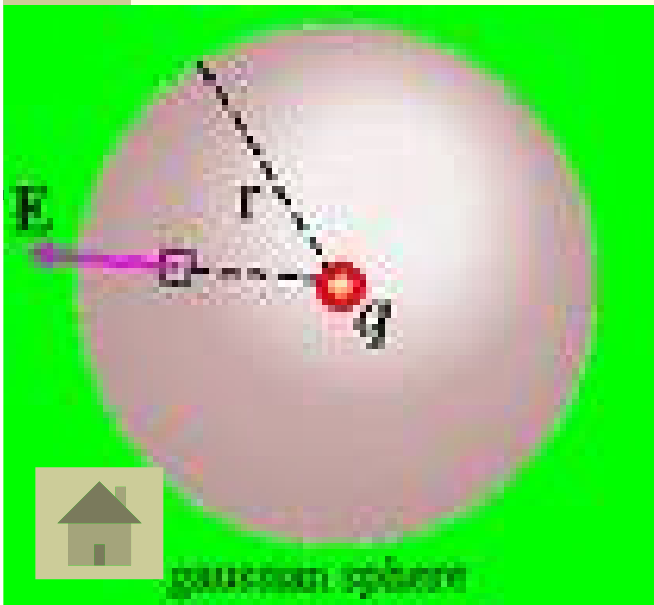


# HUKUM GAUSS

$$\Phi = EA$$

Fluks Listrik

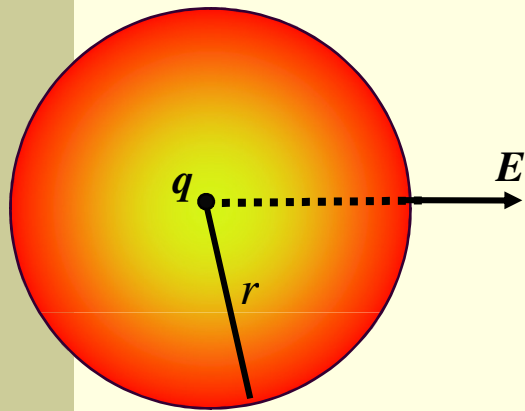
Menyatakan bahwa : Jumlah garis gaya yang keluar (fluks listrik total) dari suatu permukaan tertutup sebanding dengan jumlah muatan listrik yang dilingkupi oleh permukaan tertutup itu.



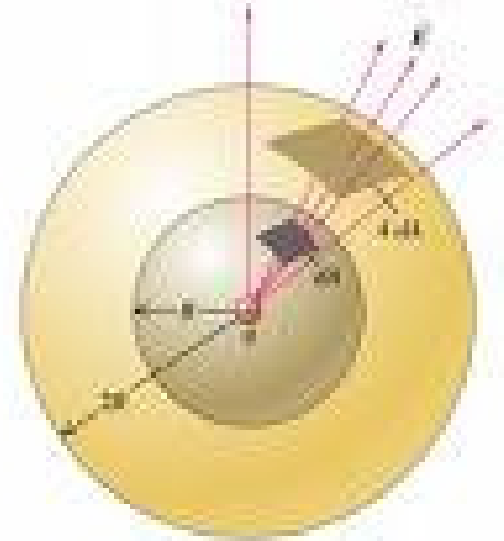
$$\Phi = \oint_s \vec{E} \cdot d\vec{A} = \sum_i \frac{q_i}{\epsilon_0} \quad s = \text{permukaan tertutup}$$

$$\Phi = \oint_s \vec{D} \cdot d\vec{A} = \sum_i q_i \quad \vec{D} = \epsilon_0 \vec{E}$$

# MEDAN LISTRIK PADA PERMUKAAN BOLA



$$\Phi = \oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$$

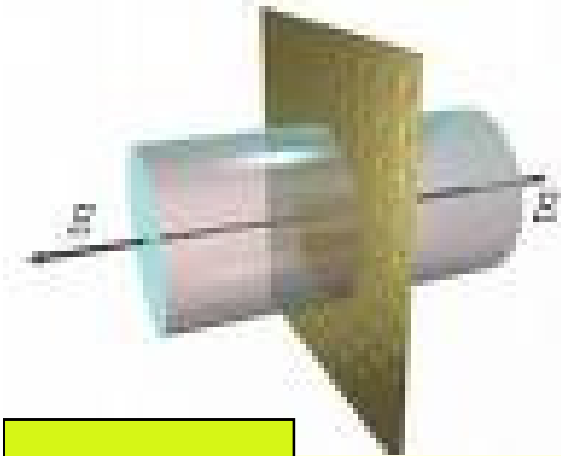


$$\oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0} \quad \text{-----} \rightarrow E(4\pi r^2) = \frac{q}{\epsilon_0}$$

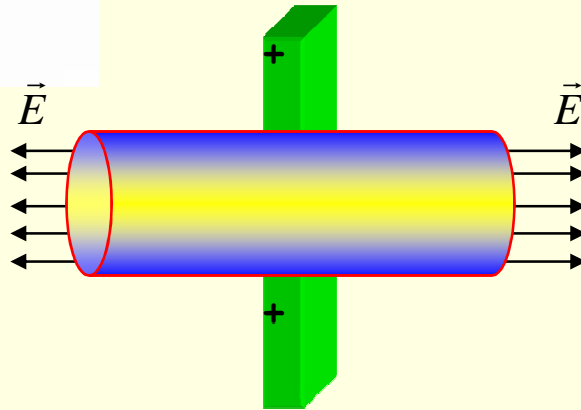
$$E = \frac{1}{4\pi r^2} \frac{q}{\epsilon_0} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \quad \text{-----} \rightarrow \vec{E} = \frac{1}{4\pi\epsilon_0} \frac{q}{r^2} \hat{r}$$



# MEDAN DI SEKITAR BIDANG BERMUATAN



$$\sigma = \frac{q}{A}$$

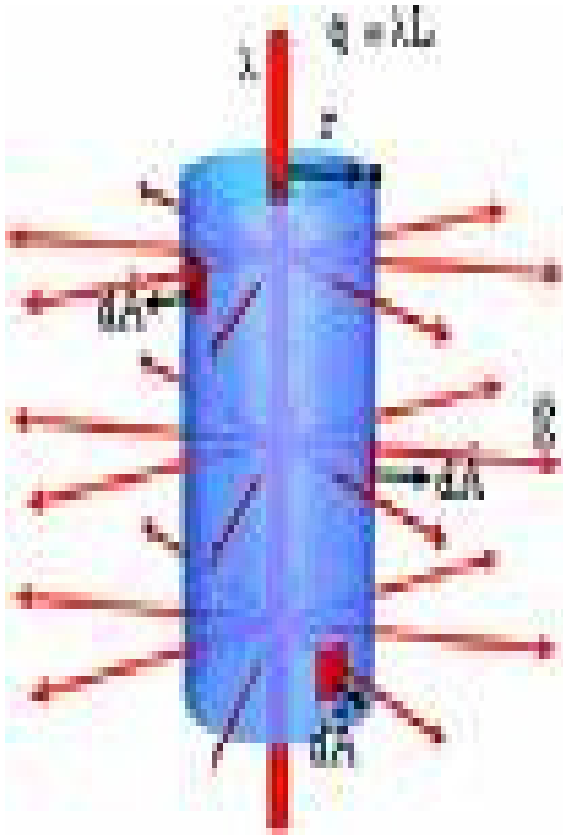


$$\oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0} \quad \text{---} \quad \rightarrow \quad \sigma = \frac{q}{A}$$

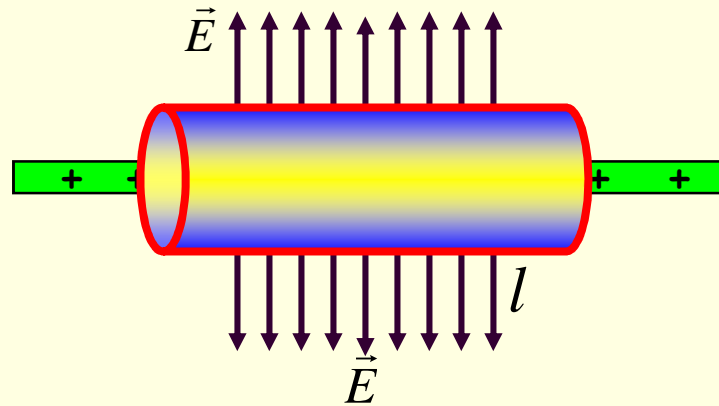
$$2AE = \frac{\sigma A}{\epsilon_0} \quad \text{---} \quad \rightarrow \quad E = \frac{\sigma}{2\epsilon_0}$$

$\sigma$  = muatan per satuan luas





# Medan Listrik di Sekitar Kawat Bermuatan Merata



$$\frac{q}{l} = \lambda$$

$$\oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0}$$

$$E (2\pi r) l = \frac{q}{\epsilon_0} \text{ ----- } > \frac{q}{l} = \lambda$$

$$E = \frac{\lambda}{2\pi r \epsilon_0} = \frac{1}{2\pi \epsilon_0} \frac{\lambda}{r}$$

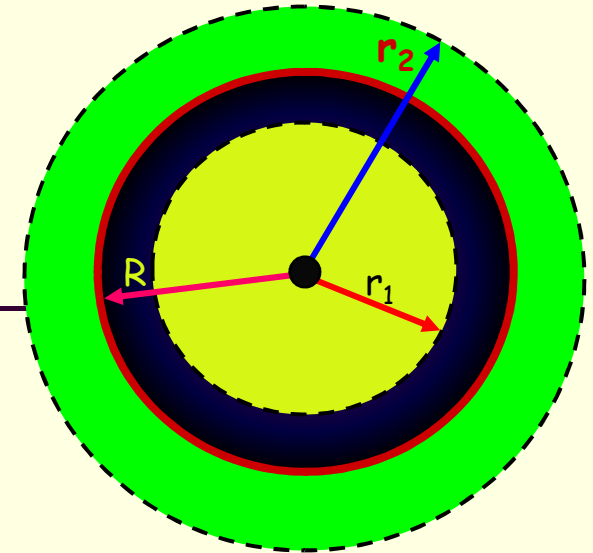
$\lambda$  = muatan per satuan panjang



# Medan Listrik Pada Bola Bermuatan

Bola isolator bermuatan merata dengan rapat muatan :

$$\rho = \frac{Q}{V} = \frac{Q}{(4/3)\pi R^3} = \frac{3Q}{4\pi R^3}$$



Di Dalam Bola

$$\oint_{s_1} \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0} \quad \text{---} \rightarrow q = \text{Muatan yang dilingkupi } s_1$$

$$\text{-----} \rightarrow q = \rho V_1 = \rho((4/3)\pi r_1^3)$$

$$E(4\pi r_1^2) = \frac{\rho((4/3)\pi r_1^3)}{\epsilon_0}$$

$$E = \frac{\rho r_1}{3\epsilon_0} \text{-----} \rightarrow \rho = \frac{Q}{V} = \frac{3Q}{4\pi R^3}$$

$$E(r) = \frac{Q}{4\pi\epsilon_0} \frac{r_1}{R^3} \text{---} \rightarrow \text{Untuk } r < R \text{ (di dalam bola)}$$

Di Luar Bola

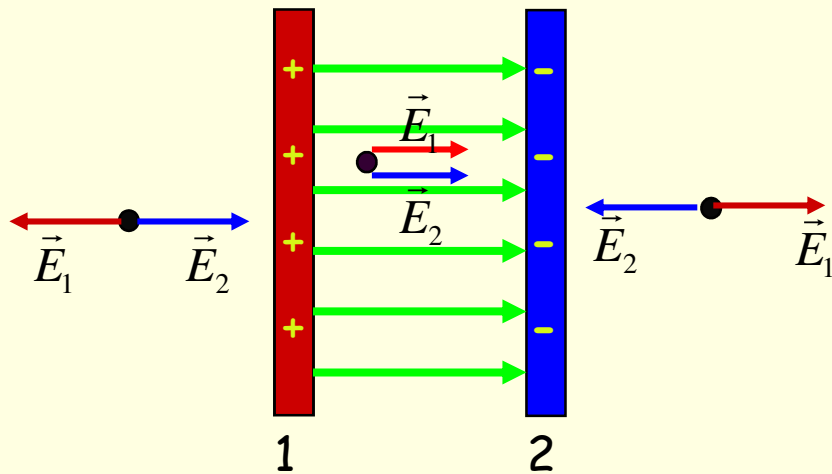
$$\oint_{s_2} \vec{E} \cdot d\vec{A} = \frac{Q}{\epsilon_0}$$

$$E(4\pi r_2^2) = \frac{Q}{\epsilon_0}$$

$$E = \frac{1}{4\pi\epsilon_0} \frac{Q}{r_2^2}$$



# MEDAN DI SEKITAR BIDANG BERMUATAN



$$\oint \vec{E} \cdot d\vec{A} = \frac{q}{\epsilon_0} \quad \text{---} > \quad \sigma = \frac{q}{A}$$

$$AE = \frac{\sigma A}{\epsilon_0}$$

$$E = \frac{\sigma}{\epsilon_0}$$

$\sigma$  = muatan per satuan luas

